

#1 Domain : $\ln(15 - x^2 - 15y^2)$ is only defined when $15 - x^2 - 15y^2 > 0$.

Therefore, the domain is $\{(x, y) : 15 - x^2 - 15y^2 > 0\}$

Range: The maximum $\ln(15 - x^2 - 15y^2)$ can be is $\ln(15)$ [when $x=y=0$].

The minimum is limitless! So our range is $(-\infty, \ln(15)]$

#2

Consider the path along $x=0$

$$\lim_{(x,y) \rightarrow (0,0)} \frac{x - 9y}{18y + 5x} = -\frac{1}{2}$$

Consider the path along $y=0$

$$\lim_{(x,y) \rightarrow (0,0)} \frac{x - 9y}{18y + 5x} = \frac{1}{5}$$

Since the limit along different paths is not the same, the limit DNE.