

$$2) f(x) = -2 \sin x \quad \text{at } x = \frac{3\pi}{4}$$

$$f\left(\frac{3\pi}{4}\right) = -2 \sin\left(\frac{3\pi}{4}\right) = -2 \cdot \frac{\sqrt{2}}{2} = -\sqrt{2}$$

$$f'(x) = -2 \cos x$$

$$f'\left(\frac{3\pi}{4}\right) = -2 \cos\left(\frac{3\pi}{4}\right) = -2 \cdot -\frac{\sqrt{2}}{2} = \sqrt{2}$$

$$y + \sqrt{2} = \sqrt{2} \left(x - \frac{3\pi}{4}\right)$$

$$y = \sqrt{2}x - \frac{3\pi}{4}\sqrt{2} - \sqrt{2}$$

$$6) f(x) = (\sin x + 2 \tan x)(\sec x - 3 \csc x)$$

$$\begin{aligned} f'(x) &= (\sin x + 2 \tan x)(\sec x \tan x + 3 \sec x \cot x) \\ &\quad + (\sec x - 3 \csc x)(\cos x + 2 \sec^2 x) \end{aligned}$$

$$4) f(x) = \frac{x - \cos x}{x^2 + \cot x}$$

$$f'(x) = \frac{(x^2 + \cot x)(1 + \sin x) - (x - \cos x)(2x - \csc^2 x)}{(x^2 + \cot x)^2}$$

$$5) f(x) = \frac{x^2 + 8\sec x}{x - 2e^x}$$

$$f'(x) = \frac{(x-2e^x)(2x + \sec x \tan x) - (x^2 + 8\sec x)(1-2e^x)}{(x-2e^x)^2}$$

$$f(x) = \begin{cases} \sin x, & x < 0 \\ 1 - \cos x, & x \geq 0 \end{cases}$$

$$\lim_{x \rightarrow 0^+} \frac{f(x) - f(0)}{x-0} \stackrel{?}{=} 1 \quad \lim_{x \rightarrow 0^-} \frac{f(x) - f(0)}{x-0} = 0$$

not continuous

$$\sin(0) = 0 \quad 1 - \cos(0) = 0$$

not differentiable

$$f(1) = 2 \quad g(1) = 2 \quad f'(1) = 1 \quad f'(2) = 3$$

$$g'(1) = 6 \quad g'(2) = 4$$

Find $F'(1)$ if $F(x) = f(g(x))$

$$F'(x) = f'(g(x)) \cdot g'(x)$$

$$F'(1) = f'(g(1)) \cdot g'(1) = f'(2) \cdot 6 = 3 \cdot 6 = 18$$