

## Homework 1

Due Wednesday, September 6, in class

**Reading.** Munkres §1 – §7, §9

**Problems.**

- §5 #3. Let  $A = A_1 \times A_2 \times \dots$  and  $B = B_1 \times B_2 \times \dots$ 
  - (a) Show that if  $B_i \subset A_i$  for all  $i$ , then  $B \subset A$ .
  - (b) Show the converse of (a) holds if  $B$  is nonempty.
  - (c) Show that if  $A$  is nonempty, each  $A_i$  is nonempty. Does the converse hold? *Comment: No need to answer this question about the converse.*
  - (d) What is the relation between the set  $A \cup B$  and the cartesian product of the sets  $A_i \cup B_i$ ? What is the relation between the set  $A \cap B$  and the cartesian product of the sets  $A_i \cap B_i$ ? *Comment: No need to prove your answer.*
- §6 #3. Let  $X$  be the two-element set  $\{0, 1\}$ . Find a bijective correspondence between  $X^\omega$  and a proper subset of itself.
- §6 #4a. Let  $A$  be a nonempty finite simply ordered set.
  - (a) Show that  $A$  has a largest element. [*Hint: Proceed by induction on the cardinality of  $A$ .*]
- §7 #3. Let  $X$  be the two-element set  $\{0, 1\}$ . Show there is a bijective correspondence between the set  $\mathcal{P}(\mathbb{Z}_+)$  and the cartesian product  $X^\omega$ .

**Recommend Problems (not to turn in).**

- §6 #2.
- §7 #4.
- §7 #5ef.