

Name:

Solutions

MAC 2311 - Analytical Geometry and Calculus I  
Quiz # 2, January 23, 2024

Problem 1 .

Given the graph of a function  $f$  state the value of each quantity below:

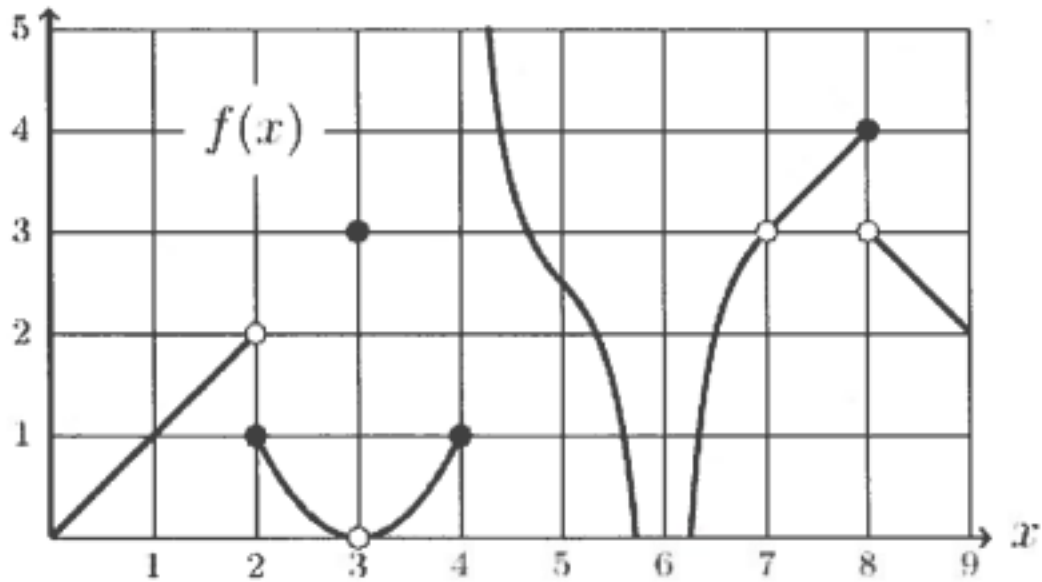


Figure 1: Graph of  $f$

(4 points)

1.

$$f(2) = 1$$

5.

$$\lim_{x \rightarrow 6^-} f(x) = -\infty$$

2.

$$\lim_{x \rightarrow 2^-} f(x) = 2$$

6.

$$\lim_{x \rightarrow 4^-} f(x) = 1$$

3.

$$\lim_{x \rightarrow 2^+} f(x) = 1$$

7.

$$\lim_{x \rightarrow 8} f(x) \text{ DNE}$$

4.

$$\lim_{x \rightarrow 2} f(x) \text{ DNE}$$

8.

$$f(8) = 4$$

**Problem 2 .**

Evaluate the following limits

**(2 points)**  
1.

$$\lim_{x \rightarrow 0} \frac{8((x-3)^2 - 9)}{x}$$

$$\lim_{x \rightarrow 0} \frac{8(x^2 - 6x + 9 - 9)}{x} \quad (1 \text{ point})$$

$$= \lim_{x \rightarrow 0} \frac{8x(x-6)}{x}$$

$$= \lim_{x \rightarrow 0} 8(x-6) = \underline{-48} \quad (1 \text{ point})$$

**(4 points)**  
2.

$$\lim_{x \rightarrow 0} \frac{\frac{1}{3+x} - \frac{1}{3}}{x}$$

Find common denominator: (2 points)

$$\lim_{x \rightarrow 0} \frac{3 - (3+x)}{3(3+x)} \cdot \frac{1}{x}$$

$$= \lim_{x \rightarrow 0} \frac{-x}{3(3+x)} \cdot \frac{1}{x} \quad (1 \text{ point})$$

$$= \lim_{x \rightarrow 0} \frac{-1}{3(3+x)}$$

$$= \underline{\frac{-1}{9}} \quad (1 \text{ point})$$