

Solutions

MAA 2311 - Calculus I
Quiz # 1, August 31, 2023

(3 points)

Problem 1 Find the domain for each the following functions. Specify the domain using interval notation or inequalities.

a)

$$f(x) = \ln(x^2 + 1)$$

(2)

• Requirement: $x^2 + 1 \geq 0$.

But this holds for any x in $(-\infty, \infty)$

Therefore the domain of f is $(-\infty, \infty)$: interval notation.
or $-\infty < x < \infty$: inequality.

(2 points)

b)

$$g(x) = \frac{2|x| + x}{x - 3}$$

(1)

The only restriction is $x \neq 3$.

Domain of g is $(-\infty, 3) \cup (3, \infty)$

Problem 2 : Solve for x (4 points)

df

Start Here

$$2\ln(x) - \ln(3-x) = \ln\left(\frac{1}{2}\right) + \ln(8)$$

(4)

$$\ln(x^2) - \ln(3-x) = \ln\left(\frac{1}{2}\right) + \ln(8) \quad (*)$$
$$\ln\left(\frac{x^2}{3-x}\right) = \ln\left(\frac{1}{2}\right) + \ln(8) = \ln(4) \quad , \log(x) - \log(y) = \log\left(\frac{x}{y}\right) \quad (1 \text{ point})$$
$$\ln\left(\frac{x^2}{3-x}\right) = \ln(4)$$

$$\frac{x^2}{3-x} = 4$$

Apply ln being one-to-one. (1 point), or take the inverse on both sides.

$$\frac{x^2}{3-x} - 4 = 0$$

$$\frac{x^2 - 4(3-x)}{3-x} = 0$$

$$(*) \ln\left(\frac{1}{2}\right) + \ln(8)$$
$$= \ln\left(\frac{1}{2} \cdot 8\right)$$
$$= \ln(4) \quad (1 \text{ point})$$

$$\frac{x^2 - 12 + 4x}{3-x} = 0$$

$$x^2 + 4x - 12 = 0$$

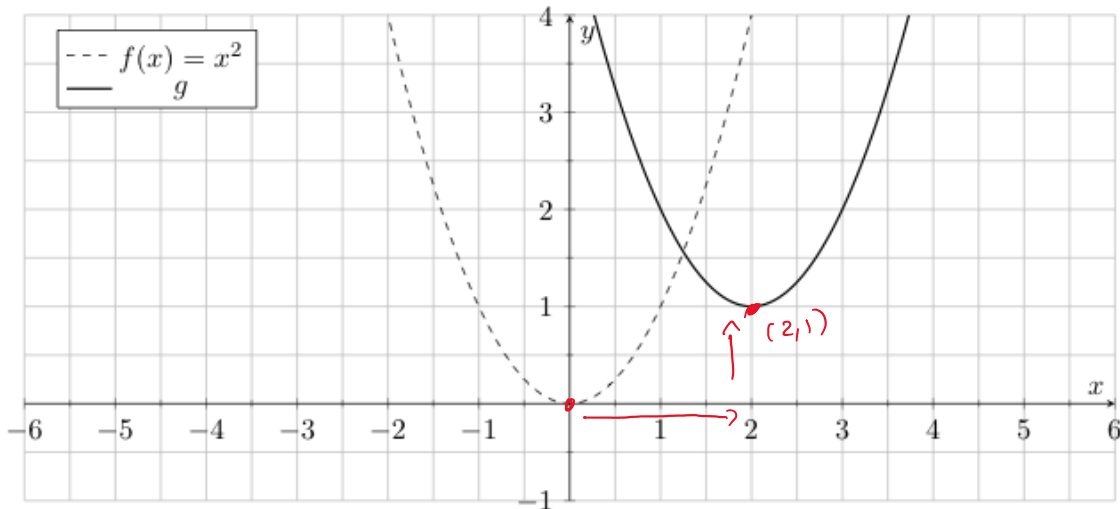
$$(x+6)(x-2) = 0$$

$$x = -6, \quad x = 2$$

- Determine that $x=2$ is the only solution because $\ln(x)$ is not defined for $x=-6$.

Problem 3 : (3 points)

Consider the graphs of the two functions f and g . Where g is obtained by transforming f .



a) Which of the following is the correct definition for g ? Choose the correct solution:

i) $g(x) = x^2 + 4x + 5$

ii) $g(x) = x^2 - 4x + 5$

iii) $g(x) = x^2 + 4x - 5$

iv) $g(x) = x^2 - 4x + 3$

$(x-2)^2 + 1 = x^2 - 4x + 4 + 1$ (2)
 shift 2 units to the right
 shift one unit upward.

b) What is the range of g ? Choose the correct solution:

i) $[1, \infty)$

ii) $(-\infty, \infty)$

iii) $(0, \infty)$

iv) $(1, \infty)$

The function g can only achieve values greater than or equal to 1. (1)