

$$\frac{d}{dx} e^x = e^x$$

Taylor series

$$\frac{d}{dx} e^x = 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + \dots$$

$$= 1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \dots$$

HW¹⁰ #7)

$$f(x) = 2\sin(x)$$

$$x = \frac{3\pi}{4}$$

$$y = 2\sin\left(\frac{3\pi}{4}\right)$$

$$f'(x) = 2\cos(x)$$

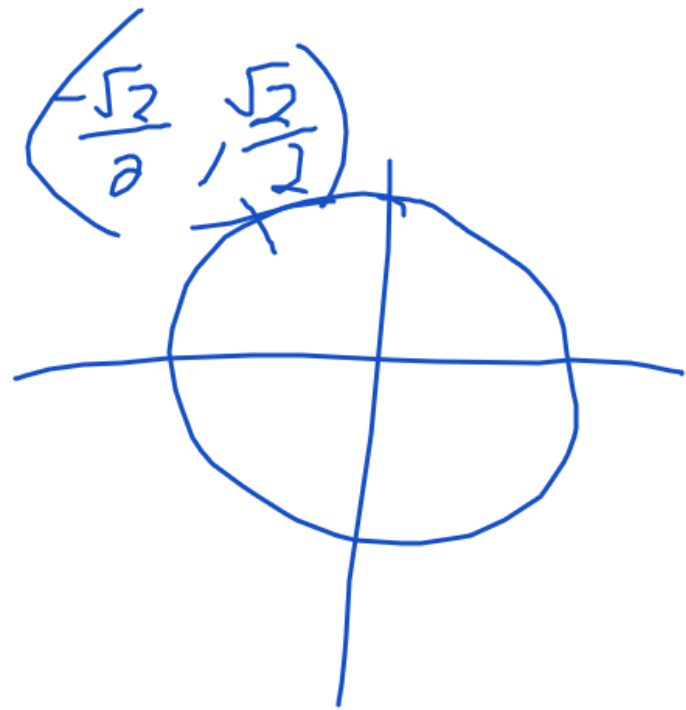
$$= 2\frac{\sqrt{2}}{2} = \sqrt{2}$$

$$f'\left(\frac{3\pi}{4}\right) = 2\cos\left(\frac{3\pi}{4}\right)$$

$$\left(\frac{3\pi}{4}, \sqrt{2}\right)$$

$$= 2\left(\frac{-\sqrt{2}}{2}\right) = -\sqrt{2} = m$$

$$y - \sqrt{2} = -\sqrt{2}\left[x - \frac{3\pi}{4}\right]$$



$$y = e^{3x} \sin^{-1}(3x-2)$$

$$y' = \left(\frac{d}{dx} e^{3x} \right) \sin^{-1}(3x-2) + e^{3x} \left(\frac{d}{dx} \sin^{-1}(3x-2) \right)$$

$$= 3e^{3x} \sin^{-1}(3x-2) + e^{3x} \left(\frac{3}{\sqrt{1-(3x-2)^2}} \right)$$

$$\begin{aligned} \frac{d}{dx} \sin^{-1}(\star) &= \frac{1}{\sqrt{1-(\star)^2}} \cdot (\star)' \\ &= \frac{3}{\sqrt{1-(3x-2)^2}} \end{aligned}$$

$$\boxed{-9} = \underline{3x^2y^3} + \underline{x \tan(y)}$$

Solve for $\frac{dy}{dx}(y)$

$$0 = 3(2x)y^3 + 3(x^2)(3y^2)\frac{dy}{dx} + \tan(y) + x \sec^2(y)\frac{dy}{dx}$$

$$0 = 6xy^3 + \underline{9x^2y^2\frac{dy}{dx}} + \tan(y) + \underline{x \sec^2(y)\frac{dy}{dx}}$$

$$-9x^2y^2\frac{dy}{dx} - x \sec^2 y \frac{dy}{dx} = 6xy^3 + \tan y$$

$$\boxed{\frac{dy}{dx}} \left[\cancel{-9x^2y^2 - x \sec^2 y} \right] = \frac{6xy^3 + \tan y}{\cancel{-9x^2y^2 - x \sec^2 y}}$$

$$\boxed{\frac{6xy^3 + \tan y}{-9x^2y^2 - x \sec^2 y}}$$

$$y = x^{2\cos(3x)}$$

solve for y'

$$\ln(y) = \ln(x^{2\cos(3x)})$$

$$\ln(y) = 2\cos(3x)\ln(x)$$

$$\left(\frac{1}{y} \cdot y' = 2(-3\sin(3x))\ln(x) + 2\cos(3x) \cdot \frac{1}{x} \right) \cdot y$$

$$y' = \left[-6\sin(3x)\ln(x) + \frac{2\cos(3x)}{x} \right] \underbrace{x^{2\cos(3x)}}_y$$

$$\sqrt{\frac{x+1}{x^2-1}} \rightarrow \ln\left(\left(\frac{x+1}{x^2-1}\right)^{1/2}\right) = \frac{1}{2} \ln\left(\frac{x+1}{x^2-1}\right)$$

$$\ln(x^a) = a \ln(x)$$

$$\ln(xy) = \ln(x) + \ln(y)$$

$$\ln\left(\frac{x}{y}\right) = \ln(x) - \ln(y)$$

$$\frac{1}{2} \ln(x+1) - \frac{1}{2} \ln(x^2-1)$$