

$$\frac{d}{dx} e^x = e^x$$

Taylor series

$$\begin{aligned} \frac{d}{dx} e^x &= \left(1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \frac{1}{120}x^5 + \dots \right) \\ &= \left(1 + x + \frac{1}{2}x^2 + \frac{1}{6}x^3 + \frac{1}{24}x^4 + \dots \right) \end{aligned}$$

$$y = e^{3x} \sin^{-1}(3x-2)$$

$$y' = 3e^{3x} (\sin^{-1}(3x-2)) + e^{3x} \frac{d}{dx} [\sin^{-1}(3x-2)]$$

$$\begin{aligned} \frac{d}{dx} \sin^{-1}(\star) &= \frac{1}{\sqrt{1-(\star)^2}} \cdot (\star)' \\ &= \frac{1}{\sqrt{1-(3x-2)^2}} \cdot \underbrace{(3x-2)'}_3 = \frac{3}{\sqrt{1-(3x-2)^2}} \end{aligned}$$

$$-9 = \underline{3x^2y^3} + \underline{x \tan(y)} \quad \text{solve for } \frac{dy}{dx} \quad (y')$$

$$0 = 3(2x)y^3 + 3(x^2)(3y^2)\frac{dy}{dx} + \tan(y) + x \sec^2(y)\frac{dy}{dx}$$

$$0 = 6xy^3 + \underline{9x^2y^2} \frac{dy}{dx} + \tan y + x \sec^2 y \frac{dy}{dx}$$

$$-9x^2y^2 \frac{dy}{dx} - x \sec^2 y \frac{dy}{dx} = 6xy^3 + \tan y$$

$$\frac{dy}{dx} \left[\cancel{-9x^2y^2 - x \sec^2 y} \right] = \frac{6xy^3 + \tan y}{\cancel{-9x^2y^2 - x \sec^2 y}}$$

$$y = x^{2\cos(3x)}$$

Solve for y'

$$\ln(y) = \ln(x^{2\cos(3x)})$$

$$\ln(y) = 2\cos(3x) \ln(x)$$

$$\left(\frac{1}{y}\right) \cdot y' = 2 \left(\underbrace{-3\sin(3x)}_{\text{product rule}} \ln(x) + \underbrace{2\cos(3x)}_{\text{product rule}} \cdot \underbrace{\frac{1}{x}}_{\text{product rule}} \right) y$$

$$y' = \left[-6\sin(3x) \ln(x) + \frac{2\cos(3x)}{x} \right] (x^{2\cos(3x)})$$

$$\rightarrow \cos(3x) = -\sin(3x) \cdot 3$$

$$y = x^2$$

$$\ln(y) = \ln(x^2)$$

$$\ln(y) = 2 \ln(x)$$

$$\frac{1}{y} \cdot y' = 2 \cdot \frac{1}{x}$$

$$y' = \frac{2}{x} \cdot y$$

$$= \frac{2}{x} \cdot x^2 = \boxed{2x}$$