

$$y = \cos(x)^{\ln(x)}$$

$$\ln y = \ln[\cos(x)^{\ln(x)}]$$

$$\ln y = \ln(x) \ln[\cos(x)]$$

$$\left(\frac{1}{y}\right) y' = \left[\frac{1}{x} \ln[\cos(x)] + \ln(x) \frac{1}{\cos(x)} \cdot (-\sin(x))\right] \cdot y$$

$$y' = \left[\frac{1}{x} \ln[\cos(x)] - \ln(x) \tan(x)\right] \cos(x)^{\ln(x)}$$

$$\text{ex) } y = \ln(x)^{\cos(x)}$$

$$\ln(y) = \ln \left[ \ln(x)^{\cos(x)} \right]$$

$$\ln(y) = \cos(x) \ln[\ln(x)]$$

$$\left[ \frac{1}{y} y' \right] y = \left[ -\sin(x) \ln[\ln(x)] + \cos(x) \frac{1}{x \ln(x)} \right] y$$

$$y' = \left[ -\sin(x) \ln[\ln(x)] + \frac{\cos(x)}{x \ln(x)} \right] \ln(x)^{\cos(x)}$$

$$s(t) = \frac{1}{3}t^3 - \frac{1}{2}t^2 - 6t + 5$$

1)  $t$  where standing still  $\rightarrow t = 3$

2) forward  $\rightarrow (3, \infty)$

3) backward  $\rightarrow [0, 3)$

$$v(t) = t^2 - t - 6$$

$$0 = (t-3)(t+2)$$

$$t = 3, t = -2$$



$$v(1) = 1^2 - 1 - 6 = -6 < 0$$

$$v(4) = 4^2 - 4 - 6 = 16 - 10 = 6 > 0$$

$$G = \underbrace{x^2 y} + \underbrace{e^{xy}} + \underbrace{\tan(y)} + \underbrace{\ln(xy^2)}$$

$$0 = \underbrace{2xy + x^2 \frac{dy}{dx}} + \underbrace{e^{xy} \left[ y + x \frac{dy}{dx} \right]} + \underbrace{\sec^2(y) \frac{dy}{dx}} + \underbrace{\frac{1}{xy^2} \left[ y^2 + 2xy \frac{dy}{dx} \right]}$$

$$-2xy - e^{xy} y - \frac{1}{x} = \left[ x^2 + e^{xy} x + \sec^2(y) + \frac{2}{y} \right] \frac{dy}{dx}$$

$$\frac{dy}{dx} = \frac{-2xy - e^{xy} y - \frac{1}{x}}{x^2 + e^{xy} x + \sec^2 y + \frac{2}{y}}$$