## Remember to show all of your work.

Problem 1. Let $f(x)=x^{3} e^{x}$
(a) Find all critical points of $f(x)$.
(b) Determine the intervals on which $f(x)$ is increasing or decreasing.
(c) Find all potential inflection points of $f(x)$.

Problem 2. For each part below, answer "yes" or "no" and provide a short(!) explanation why.
(a) Does the Mean Value Theorem hold for $f(x)=\cos (x) \ln (x)$ on the interval $[0,2 \pi]$ ?
(b) Does Rolle's Theorem hold for $f(x)=x-\frac{1}{x}$ on the interval $[1,2]$ ?

