March 30, 2021

Remember to show all of your work.

Problem 1. (9 points) Let $f(x) = \frac{x^3 - 16}{x}$. Then $f'(x) = \frac{2x^3 + 16}{x^2}$ and $f''(x) = \frac{2x^3 - 32}{x^3}$.

- (a) Determine the domain of f(x).
- (b) Find any vertical / horizontal asymptotes of f(x), if they exist.
- (c) Identify any possible critical points.
- (d) Find the intervals on which f(x) is increasing / decreasing.
- (e) Identify any possible inflection points.
- (f) Find the intervals on which f(x) is concave up / concave down.

(g) Graph f(x) approximately (label any critical points, inflection points, asymptotes).

Hint: You can use the approximation $\sqrt[3]{16} \approx 2.5$

Problem 2. (1 point) In honor of April Fool's Day on Thursday, what's your favorite joke / pun?