

- ▶ JAKE PARDO, *Gambling against some odds.*

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A restricted value martingale is a martingale whose increments take their magnitude from a given set of positive real numbers S – we call any such martingale an S -martingale. A set B anticipates a set A if every A -martingale is dominated by a countable set of B -martingales, and A evades B if this is not the case. Similarly, B singly anticipates A if every A -martingale is dominated by a single B -martingale, and otherwise A singly evades B . Bavly and Peretz investigated the anticipation/evasion relationships between various sets of real numbers and in the process solved the case where $\sup A$ is bounded and B is bounded away from 0 and the case where B is well-ordered. This left a big question: what happens when 0 is an accumulation point of B ?

I will prove that the natural numbers \mathbb{N} singly evade the set $\{x^{-n} : n \in \mathbb{Z}\}$, where x is any positive real number. The proof is based on a betting game between two gamblers, one using an A -martingale as a strategy and the other using a B -martingale, in which a strategy for the A -martingale gambler is produced. The proof has an interesting connection to the n -Fibonacci numbers.