

the points that make the derivative zero and/or the points that make the derivative undefined (provided that they are in the domain). These points are called *critical points*. Endpoints of the interval may or may not give rise to an extremum, or a relative extremum, of the function.

The following one-dimensional version of the inverse function theorem states that a differentiable function f is invertible (i.e., has an inverse) in a neighborhood of any point x at which $f'(x) \neq 0$, and its inverse is differentiable.

THEOREM 5.2.8. (*Inverse Function Theorem*) Suppose that I is an interval and a function $f : I \rightarrow \mathfrak{R}$ is differentiable with $f'(x) \neq 0$, for any $x \in I$. Then

(a) f is an injection,

(b) f^{-1} is continuous on $f(I)$,

(c) f^{-1} is differentiable on $f(I)$, and

(d) $(f^{-1})'(y) = \frac{1}{f'(x)}$, with $y = f(x)$. This may be written as $\frac{dx}{dy} = \frac{1}{\frac{dy}{dx}}$.