

Proof of the mean value theorem. Consider a new function g defined by

$$g(x) = f(x) - \frac{f(b) - f(a)}{b - a}x.$$