MHF 3202, Dr. Block, Problem Set 2, Spring 2020

1. Suppose that A, B, and C are sets. Prove that

$$(A \cup C) \subseteq (B \cup C)$$

if and only if

$$(A-C)\subseteq (B-C).$$

2. Prove or disprove the following:

If $a, b, c \in \mathbb{Z}$, then at least one of the three integers

$$b^2 - c^3$$
, $a^2 + b$, $c - a$

is even.