(the luks on the page material page two excellent, free on-line books . New-al Networks and Deep Learning These Le ctures are based on by Michael Nielsen

Deep Learning by GoodFellow, Benglo and Courulle

to collect answer Compare out put minibator 2 is adjusted. After all the minibatches MACHINE LEARNING BIG DICTURE DATA is SENT IN as MINI-batches, after each have been "Larned" he Fingl machine Myring is run on test data to see how often it me to rong adjust. gields correct answers. parameters n depends on Mechine Mm edure ML9 la batches training data Ĩ

 \sim F. 1+ INPUTS X' Rui and out puts az ER"141 F. (x, Ai, b,) depends on the parameters · Ai an (nux ni) matrix of weights so b an (n, x1) vector = the bias Each layer is represented by a function - Many possible Structure tor My etc. - We first cover the big math picture for an activation Function T a push Forward, Fully connected net $A: \mathbb{R}^{n_{L}} \to \mathbb{R}^{n_{L}+1}$ N2+1 NEUrows 0 0 1 1 1 pg 7 7 7g ר -ב

p (0'Z)XOM = (F) A V(2)=1+02 · ramp or ReLy The activation function has variou forms . Step fauction e Sigmoid $-(\chi, A; b_{L}) = T(A_{L} \times + b_{L})$ 4

74 GM = F_k o F_{k,1} o .. o F_{i, M} = (A_{i, b_{i, 1}} A_{2, b_{2, i-1}} A_{k_{i}} b_{k}) all the weights and blue together (lots of Putting the pieces to gether from many layers · Reactivation function is vectorized, ie. < (('\$') ~ ('\$') = (T(\$') · , T(\$'))</pre> It acts on each componet of a vector 1 1 7 0 0 0 7 7 7 0 0 0 7 7 7 0 0 0 T and F. Rut -> Rutti Parameters!). Q 6 ę

data Z1, , XN Which are correctly characterized (This is simplest, least squares version. More $\mathcal{F}_{\mathbf{x}_{1}}^{\mathbf{x}_{1}} = \frac{1}{\mathbf{x}_{1}} \left[\mathcal{F}_{\mathbf{x}_{1}}^{\mathbf{x}_{1}} \right] = \frac{1}{\mathbf{x}_{1}} \left[\mathcal{F}_{\mathbf{x}_{1}}^{\mathbf{x}_{1}} \right] - \mathcal{F}_{\mathbf{x}_{1}}^{\mathbf{x}_{1}} \right]$. Now we train the Machine with training and use an optimization Broutline t We treat this as a function of my Now throw in all the training data and Construct the costor objective or error Sophisticated versions later dimiush many in to An. Repeat with 2 - 37. 45 J1,... Jn. Function

Now he question is why For takes · This is connected to why it is called a The goal is to get a My given by Gyr that generalized it. Works well on Stest A big ISJUR IS how much to optimize by the machine to memorize the training deter and not generalize to other test data data is thrown in, or is adjusted, then another · In pradize, a radown subset of training for Just the trainglug set, Don't want data that is not in the trainingset This is called over-Fitting neurel net Lhis Form? minibetch, etc. 0

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We know a little about actual neurous It will be easier to understand the found of a neural met after ł

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V, de o on yout ube by Marc Dingman

Art. FICIAL NEWRONS and a sjugle layer het ecture MLbt

M A micshold -b is set (minus sign explained 196) . The out put is zera or one (fire or don't fire) The neuron weighs the lupyt using weights · We first describe a simple artificial Neuron called "the perceptron" - out Put also called the blas WI, W2 and W3

00 · X3 = whit your friends are doing to might · you weigh up these various factors and E xample: you are trying to decide whether to do your math Hwytenight We want to express the decision process · X, = how close is the due date male a decision o= no, 1=yes. · X2 = how long is the Hw $w_1 x_1 + w_2 x_2 + w_3 x_3 > - b$ d-2 Exentex wt 1x m more succluctly. out put is one it out put is zero if · Kule! Q

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| activation function | $P\left[\frac{1}{2} + \frac{1}{2} + \frac{1}{2}\right] = \frac{1}{2} + \frac{1}{2} +$ | | in we want to model a more complicated in we want to model a more complicated | | | | |
| act109 | te th | yes. | more ler pr | · · · | | x x x | |
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| 1 v v v v | H 13 | 011 (x) | te ma | perceptron | P On P | | 50 075 |
| 071 | | | turn | e per | | ` <i>[\]</i> . | // |
| N 12) - C | t F(x) = | nont | 3 | multiple | | X | × Ko |
| et | L' | F | Now | M | | | |

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2 K=1, M=# & neurons into a matrix For ere the the kith perception has weights 2 M , wa n H 5 + 1× Wk and mreshold or blas bik $\begin{pmatrix} x^{4} + x + x^{+} \\ x^{-1} + y \end{pmatrix} = \begin{pmatrix} x^{-1} + y^{+} \\ x^{-1} \end{pmatrix}$ We want to combue all these 1-0 13. [) کر کر we get for each k 13.4 Wm x + bm $|w_{1}x_{1}x_{2}+b_{1}|$ $\frac{1}{19} + \frac{1}{1} \times \frac{1}{10}$ Let W=1 11 thew Ø Q

11/ The last step is to vectorize the adjunction T We now change our point of view on our one layer machine is described by the one layer is perceptions and treat · So letting A= W, he weight watrix It as a learning Machine F(x) = T(Ax + b)TE1) T (2) m 11 47 TX . 6

earning anad Mutryle Layes \sum lecture

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| to isci | Muchin (| 5 quare | Arth |
| harac | arameter $\frac{1}{x_1} + \frac{1}{b_1}$ | | × 2 W 2 W 1 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 |
| we return to the characterization proven Li so Zi, , Xi, and inputs with correct to out puts di, 42, , yi | of the parameters (the with the muchine output) X Input the muchine output) = T (AX + b) | • For each i , n_{15} has least squares error $E_{L} = (AX_{L} + b) - J_{L} ^{2}$ | Fotal Error over an an an A (A, b) - r M M. A (A, b) - g (A, tb) - g, I (A, tb) - g, I ~ |
| 41 12 X 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 | a value of for each | 1, ms | fot a (A, b) |
| we return to so X1, ; XN av outputs B1, 43 | Fix a value o and for each | - H Gack | Foi te tot gi |
| S S E | We f | e Foi | e I |
| 9 9 9 | | | |
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 \mathcal{E}' · Now we optimize, it find Arad by which MINIMIZE DENDED D (A, J) Looking more closely, how do we We new declare our Flug I machine to Note the Similarity to leest squares and puly no mial Filting USUAL Ming is to differentiat of With respect to A and b, etc. - But V is not differentiable. 6< 0 T (A, X+4) optimite? 0

14 Should I spend how med time The output is not just a on 1, but a number. S I A Another issue with T is that BACK TO The HW example restrictive, bluary outpay at c1 proj woth from close is the Friends doing due date What are my Homa おう 0

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| 0.1 | So which for a last a want 5 mall changes or maybe differentiasto we want 5 mall changes in the output in the parameter to yield swall changes in the output | · De signoid T(2)= 1+E-2 T(2)=0 as 23-00 Is wice and differtially expensive the stand | by computation of the second to be the second of the ramp T(2) = MAX(2,0) | 15 continuous, its "derivative" 15 3 Which is not so bad | and 15 computationally tame. | Wa don't need to speen the actuation function to but sweetingty we with the mature to the section of a section of the section | Tor Now let Tbe to sigmoid tor memory of |

let's study optimization or learning for one level and if the trans values are 31 and 92 we have $Z_{2} = T[w_{2i}x_{i} + w_{22}x_{2} + w_{23}x_{3} + b_{2})$ let's have three inputs and 2 heurous + $(T (W_{21} X_{1} + W_{22} X_{2} + W_{23} X_{3}^{+} + b_{2}) - 9_{2})^{2}$ 50 Z1 = V (W1 X1 + W2 X2 + W3 X3 + b,) F(x,A,b) = T(A,x+b;) $\oint = \left(T \left[w_{11} \, x_{1} + w_{12} \, x_{2} + w_{13} \, x_{3} + b_{1} \right) - y_{1} \right)^{2}$ 10 July ZZ ZZ X N N

but we need many layers with many nervous and For example, Vd = [Jd] , Jd, Jd, Jd, Jd, Jd, Jo, Jak, John Mars, J This is complicated for just this simple one layer and see if hey are loc wer, min or sadler compute VI and find critical points function of the parameters he wis and b's So we treat & as a function of hese We what TO MINIMIRE The Error Person a JA - r'(Same argument). & 1 2 = r'(same argument) * 1 mybe mousands of parameters. by the chain Rule. My P 50 m m gud

| | scheme namely the DD when | clever way of computer + | will cover each of these in more a locario | Fluish the Introduction we describe layers - this is the "Deep" in deep | Mis is decision |
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| need new idea | be Her Optimization scheme Gradient Descent | A clever way of co there are many layers | rev ea | st the rs - th | Learning to Thirk at one way to Thirk at making in Stages |
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| N N N | (i) A | × € (5) | We will cover in later lectures | Now to multiple | learning one way |
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trates PT T · For example, first you decide how much time decide here what order to fit it in with your to allot by your maps the tonight, then you XIQ e each layer is given by a function $F_{i}(\vec{x}, A_{i}, \vec{b}_{L}) = \nabla (A_{x} + \vec{b}_{L})$ Afurous Neurons 11 L+1 0 N, N Ö other HW. ↑ īx P 9 えな

Mana matically, this is a composition (recall it - This net is called 11 Feed Grwand " J Sivia It depends on all the Ai audbi SO VB In Formation Just Flows In one direction J = K || F(x,) - 4, || aid 15 Written 14 he reverse order) F tree F2 tree F3 ... F Then he least Squares error 15 H pyt -> ON typy H - The layers act sequentially F: FoF. C. C. FoF. 15 a Chore to compute