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Cyr

Quiz 1

You must show all work to receive full credit!!

Problem 1. (2.5 pts) Evaluate $\int 5x \sec^2(9x) dx$.

$$\begin{aligned} & 5 \int x \sec^2(9x) dx \quad \text{IBP} \quad u=x \quad dv=\sec^2(9x)dx \\ & \quad \quad \quad du=dx \quad v=\frac{1}{9}\tan(9x) \\ & = 5 \left[\frac{1}{9}x \tan(9x) - \frac{1}{9} \int \tan(9x) dx \right] \quad \text{u-sub} \quad u=\cos(9x) \\ & \quad \quad \quad du=-9\sin(9x)dx \\ & = \frac{5}{9}x \tan(9x) + \frac{5}{9} \int \frac{du}{9u} \\ & = \frac{5}{9}x \tan(9x) + \frac{5}{81} \ln|u| + C \\ & = \boxed{\frac{5}{9}x \tan(9x) + \frac{5}{81} \ln|\cos(9x)| + C} \\ & \text{(or } \frac{5}{9}x \tan(9x) - \frac{5}{81} \ln|\sec(9x)| + C) \end{aligned}$$

Problem 2. (2.5 pts) Evaluate $\int 47 \tan^3 x \sec x dx$.

$$\begin{aligned} & = 47 \int \tan^3 x \sec x dx = 47 \int \tan^2 x \sec x \tan x dx \\ & \quad \quad \quad = 47 \int (\sec^2 x - 1) \sec x \tan x dx \\ & \text{u-sub} \quad u=\sec x \quad du=\sec x \tan x dx \\ & \quad \quad \quad = 47 \int (u^2 - 1) du = 47 \left(\frac{u^3}{3} - u \right) + C \\ & \quad \quad \quad = \boxed{\frac{47}{3} \sec^3 x - 47 \sec x + C} \end{aligned}$$