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MAC 2313.8443
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Quiz 5

You must show all work to receive full credit!!

Problem 1. (6 pts) Let $f(x, y) = \frac{x}{x+4y}$. Evaluate $f_y(3, \frac{1}{4})$ and $f_{yy}(1, \frac{1}{4})$.

$$f_y = \frac{(x+4y) \cdot 0 - x \cdot 4}{(x+4y)^2} = \frac{-4x}{(x+4y)^2} \Rightarrow f_y(3, \frac{1}{4}) = \frac{-4(3)}{(3+4 \cdot \frac{1}{4})^2} = \frac{-12}{4^2}$$
$$= \frac{-12}{16} = \boxed{\frac{-3}{4}}$$

$$f_{yy} = \frac{\partial}{\partial y} (f_y) = \frac{(x+4y)^2 \cdot 0 - (-4x) \cdot 2(x+4y) \cdot 4}{(x+4y)^4} = \frac{32x}{(x+4y)^3}$$

$$\Rightarrow f_{yy}(1, \frac{1}{4}) = \frac{32 \cdot 1}{(1+4 \cdot \frac{1}{4})^3} = \frac{32}{8} = \boxed{4}$$

Problem 2. (4 pts) Let $g(x, y) = \frac{x^2}{x^2 + y^2}$.

(a) Evaluate $\lim_{(x,y) \rightarrow (0,0)} g(x, y)$ along the x -axis.

Along the x -axis, $y=0$, so

$$\lim_{x \rightarrow 0} \frac{x^2}{x^2 + 0^2} = \lim_{x \rightarrow 0} \frac{x^2}{x^2} = \lim_{x \rightarrow 0} 1 = \boxed{1}$$

(b) Evaluate $\lim_{(x,y) \rightarrow (0,0)} g(x, y)$ along the line $y = x$.

$$\lim_{x \rightarrow 0} \frac{x^2}{x^2 + x^2} = \lim_{x \rightarrow 0} \frac{x^2}{2x^2} = \lim_{x \rightarrow 0} \frac{1}{2} = \boxed{\frac{1}{2}}$$

(c) What can you conclude about $\lim_{(x,y) \rightarrow (0,0)} g(x, y)$? Explain your answer.

The limit does not exist since we found two paths which approach different limits.