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 MAC 2313.9722
 Cyr

Quiz 6

You must show all work to receive full credit!!

Problem 1. (5 points) Find an equation of the tangent plane to $f(x, y) = xy^{-2}$ at the point $(-4, 2)$, and use it to approximate $f(-4.4, 2.2)$.

$$f(-4, 2) = \frac{(-4)}{2^2} = -\frac{4}{4} = -1$$

$$f_x = y^{-2} \Rightarrow f_x(-4, 2) = \frac{1}{2^2} = \frac{1}{4}$$

$$f_y = -2xy^{-3} \Rightarrow f_y(-4, 2) = \frac{-2(-4)}{2^3} = \frac{8}{8} = 1$$

$$z = f_x(-4, 2)(x+4) + f_y(-4, 2)(y-2) + f(-4, 2)$$

$$z = \frac{1}{4}(x+4) + (y-2) - 1 \Rightarrow \boxed{z = \frac{1}{4}x + y - 2}$$

$$f(-4.4, 2.2) \approx \frac{1}{4}(-4.4) + 2.2 - 2 = -1.1 + 0.2 = \boxed{-0.9}$$

Problem 2. (5 points) Let $z = \arctan(x^2 + y^2)$, $x = u \ln(v)$, $y = ve^u$. Use the chain rule to evaluate the partial derivative $\frac{\partial z}{\partial v}$ at the point $(u, v) = (0, 1)$.

$$\frac{\partial z}{\partial v} = \frac{\partial z}{\partial x} \cdot \frac{\partial x}{\partial v} + \frac{\partial z}{\partial y} \cdot \frac{\partial y}{\partial v} \quad (u, v) = (0, 1) \Rightarrow (x, y) = (0, 1)$$

$$= \left(\frac{2x}{1+(x^2+y^2)^2} \right) \left(\frac{u}{v} \right) + \left(\frac{2y}{1+(x^2+y^2)^2} \right) (e^u)$$

$$\left. \frac{\partial z}{\partial v} \right|_{(0,1)} = \left(\frac{0}{1+1} \right) \left(\frac{0}{1} \right) + \left(\frac{2}{1+1} \right) (e^0) = \frac{2}{2} = \textcircled{1}$$