

Quiz 2 Solutions
MAC 1147.3096, Fall 2016
Thursday, September 8, 2016

Show all relevant work to support your answer. A correct answer without supporting work will not earn the points. **Problems 3 and 4 are on the back.**

1. (1 point) What is your favorite food? (Hint: There is no wrong answer)

1. _____

2. (4 points) Solve the following inequalities using interval notation:

(a) $\left| \frac{x-3}{2} \right| \geq 4$

Solution: The inequality translates to $\left(\frac{x-3}{2} \right) \geq 4 \cup - \left(\frac{x-3}{2} \right) \geq 4$.
Solving $\left(\frac{x-3}{2} \right) \geq 4$ for x , we get $x \geq 11$. As for the second inequality, we get $x \leq -5$. Hence, the solution is $(-\infty, -5] \cup [11, \infty)$.

(b) $-1 \leq \frac{-3x+5}{7} \leq 2$

Solution: Multiply all parts of the inequality by 7 to get $-7 \leq -3x+5 \leq 14$. Now subtract 5 from all parts and get $-12 \leq -3x \leq 9$. Divide everything by -3 , we then see our solution as $-3 \leq x \leq 9$ or $[3, 9]$.

3. (2 points) Solve the following equation by extracting square roots: $9x^2 = 36$.

Solution: Taking square roots of both sides, we see $3x = \pm 6$. Hence $x = \pm 2$.

4. (3 points) Solve the following radical equation for x : $2\sqrt{x+1} - \sqrt{2x+3} = 1$.

Solution: We can solve the equation in the following steps:

$$\begin{aligned}2\sqrt{x+1} - \sqrt{2x+3} &= 1 \\2\sqrt{x+1} &= 1 + \sqrt{2x+3} \\(2\sqrt{x+1})^2 &= (1 + \sqrt{2x+3})^2 \\4(x+1) &= 1 + 2\sqrt{2x+3} + (2x+3) \\4x+4 &= 2x+4 + 2\sqrt{2x+3} \\2x &= 2\sqrt{2x+3} \\x &= \sqrt{2x+3} \\x^2 &= (\sqrt{2x+3})^2 \\x^2 &= 2x+3 \\x^2 - 2x - 3 &= 0 \\(x+1)(x-3) &= 0 \\x &= -1, 3.\end{aligned}$$

Finally checking both solutions in the equation, we find 3 is the only valid solution to the problem.