

1. Evaluate:

$$\lim_{x \rightarrow 0} \frac{\sin(x)}{2x}$$

**Solution.** Given that the limit of  $\frac{\sin(x)}{x}$  is 1 as  $x \rightarrow 0$ , we have

$$\begin{aligned} \lim_{x \rightarrow 0} \frac{\sin(x)}{2x} &= \lim_{x \rightarrow 0} \frac{\sin(x)}{x} \cdot \frac{1}{2} \\ &= 1 \cdot \frac{1}{2} \\ &= \frac{1}{2}. \end{aligned}$$

$$\boxed{\frac{1}{2}}$$

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2. Find the second derivative of  $g(x) = x^3 + 3x^2 + 3x + 1$ .

**Solution.** We take the derivative of  $g$  twice.

$$\begin{aligned} g'(x) &= \frac{d}{dx} g(x) \\ &= \frac{d}{dx} (x^3 + 3x^2 + 3x + 1) \\ &= 3x^2 + 6x + 3 \implies \\ g''(x) &= \frac{d}{dx} g'(x) \\ &= \frac{d}{dx} (3x^2 + 6x + 3) \\ &= 6x + 6. \end{aligned}$$

$$\boxed{6x + 6}$$

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3. Find the derivative of  $f(x) = \cot(x) \cos(x)$ .

**Solution.** We use the product rule:

$$\begin{aligned} f'(x) &= \cot(x) \frac{d}{dx}(\cos(x)) + \frac{d}{dx}(\cot(x)) \cos(x) \\ &= \cot(x)(-\sin(x)) + (-\csc^2(x)) \cos(x) \\ &= \boxed{-\cos(x) - \cot(x) \csc(x)} \\ &= \boxed{-\frac{\cos(x)(\sin^2(x) + 1)}{\sin^2(x)}} \\ &= \boxed{-\cos(x)(1 + \csc^2(x))}. \end{aligned}$$