

MAC 2311 - Period: _____
Quiz 5 - Form A
October 6, 2015

Name: KEY
Please write your name and form on your paper.
Show your work to earn full credit.

1. State the limit definition of the derivative $f'(a)$. (2 points)
2. Given that $f(x) = \sqrt{x+5}$, use the limit definition of the derivative to compute $f'(1)$ and find an equation of the tangent line. (2 points)
3. Find the values of x where $y = x^3 + 27$ and $y = x^2 + 5x - 6$ have parallel tangent lines. (You may use the power rule to compute any necessary derivatives for this problem only). (2 points)

① $f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$ OR $f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$

② $f(1+h) - f(1) = \sqrt{(1+h)+5} - \sqrt{1+5} = \sqrt{6+h} - \sqrt{6}$

① for work $\xrightarrow{\text{mult by conjugate}} = \frac{6+h-6}{\sqrt{6+h} + \sqrt{6}} = \frac{h}{\sqrt{6+h} + \sqrt{6}}$

Then $f'(1) = \lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h} = \lim_{h \rightarrow 0} \frac{1}{\sqrt{6+h} + \sqrt{6}} = \frac{1}{2\sqrt{6}}$ ① $\frac{1}{2}$

Equation of the tangent line: $y - f(1) = f'(1)(x - 1)$
 $\Leftrightarrow y - \sqrt{6} = \frac{1}{2\sqrt{6}}(x - 1)$ ① $\frac{1}{2}$

③ Let $f(x) = x^3 + 27$ and $g(x) = x^2 + 5x - 6$. Set $f' = g'$ & solve for x . ① $\frac{1}{2}$

$f'(x) = g'(x) \Leftrightarrow 3x^2 = 2x + 5$ ① $\frac{1}{2}$ correct derivatives

$\Leftrightarrow 3x^2 - 2x - 5 = 0$

$\Leftrightarrow (3x - 5)(x + 1) = 0$

So $x = \frac{5}{3}, -1$ ① $\frac{1}{2}$

MAC 2311 - Period: _____
Quiz 5 - Form B
October 6, 2015

Name: KEY
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1. State the limit definition of the derivative $f'(b)$. (2 points)
2. Given that $f(x) = \sqrt{x+4}$, use the limit definition of the derivative to compute $f'(-1)$ and find an equation of the tangent line. (2 points)
3. Find the values of x where $y = x^3 + 8$ and $y = x^2 + 5x + 6$ have parallel tangent lines. (You may use the power rule to compute any necessary derivatives for this problem only). (2 points)

① on form A

$$\boxed{2} \quad f(-1+h) - f(-1) = \sqrt{-1+h+4} - \sqrt{-1+4} = \sqrt{h+3} - \sqrt{3}$$

① for work

Mult. by
conjugate:

$$= \frac{h+3-3}{\sqrt{h+3} + \sqrt{3}} = \frac{h}{\sqrt{h+3} + \sqrt{3}}$$

$$\text{Then } f'(-1) = \lim_{h \rightarrow 0} \frac{f(-1+h) - f(-1)}{h} = \lim_{h \rightarrow 0} \frac{1}{\sqrt{h+3} + \sqrt{3}} = \frac{1}{2\sqrt{3}} \quad \left(\frac{1}{2}\right)$$

Equation of the tangent line: $y - f(-1) = f'(-1)(x - (-1))$

$$\Leftrightarrow \boxed{y - \sqrt{3} = \frac{1}{2\sqrt{3}}(x + 1)} \quad \left(\frac{1}{2}\right)$$

③ Same as form A. (Constant terms go to zero when derivative is taken).

MAC 2311 - Period: _____
Quiz 5 - Form C
October 6, 2015

Name: KEY
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1. State the limit definition of the derivative $f'(c)$. (2 points)
2. Given that $f(x) = \sqrt{x+6}$, use the limit definition of the derivative to compute $f'(-1)$ and find an equation of the tangent line. (2 points)
3. Find the values of x where $y = x^3 - 8$ and $y = x^2 + 5x + 6$ have parallel tangent lines. (You may use the power rule to compute any necessary derivatives for this problem only). (2 points)

① Same as form A

② $f(-1+h) - f(-1) = \sqrt{-1+h+6} - \sqrt{-1+6} = \sqrt{5+h} - \sqrt{5}$

① for work Multiply by:
conjugate $= \frac{5+h-5}{\sqrt{5+h}+\sqrt{5}} = \frac{h}{\sqrt{5+h}+\sqrt{5}}$

Then $f'(-1) = \lim_{h \rightarrow 0} \frac{f(-1+h) - f(-1)}{h} = \lim_{h \rightarrow 0} \frac{1}{\sqrt{5+h} + \sqrt{5}} = \frac{1}{2\sqrt{5}} \cdot \left(\frac{1}{2}\right)$

Equation of tangent line: $y - f(-1) = f'(-1)(x - (-1))$

$\Leftrightarrow \boxed{y - \sqrt{5} = \frac{1}{2\sqrt{5}}(x + 1)} \cdot \left(\frac{1}{2}\right)$

③ Same as form A.

MAC 2311 - Period: _____
Quiz 5 - Form D
October 6, 2015

Name: KEY

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1. State the limit definition of the derivative $f'(d)$. (2 points)
2. Given that $f(x) = \sqrt{x+2}$, use the limit definition of the derivative to compute $f'(1)$ and find an equation of the tangent line. (2 points)
3. Find the values of x where $y = x^3 - 27$ and $y = x^2 + 5x - 6$ have parallel tangent lines. (You may use the power rule to compute any necessary derivatives for this problem only). (2 points)

① Same as form A.

$$\textcircled{2} \quad f(1+h) - f(1) = \sqrt{1+h+2} - \sqrt{1+2} = \sqrt{3+h} - \sqrt{3}$$

① for work

Multiply by conjugate:
$$= \frac{3+h-3}{\sqrt{3+h} + \sqrt{3}} = \frac{h}{\sqrt{3+h} + \sqrt{3}}$$

$$\text{Then } f'(1) = \lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h} = \lim_{h \rightarrow 0} \frac{1}{\sqrt{3+h} + \sqrt{3}} = \frac{1}{2\sqrt{3}} \quad \textcircled{\frac{1}{2}}$$

Equation of the tangent line:

$$\begin{aligned} y - f(1) &= f'(1)(x-1) \\ \Leftrightarrow \boxed{y - \sqrt{3} &= \frac{1}{2\sqrt{3}}(x-1)} \quad \textcircled{\frac{1}{2}} \end{aligned}$$

③ Same as form A.

Problem References:

1. Section 3.1 Summary (and used in pretty much every problem) and Webassign HW 5 #10.
2. Section 3.1 #37 and Webassign HW 5 #12.
3. Section 3.2 #52.