

Name: Solution

MAC1105 Section 1A26 Quiz 6

Please show all of your work in a NEAT and ORGANIZED fashion.

1. (3 points) Divide and write your answer in standard form $a + bi$.

$$\begin{aligned} \frac{(8-6i)}{(2-i)} \cdot \frac{(2+i)}{(2+i)} &= \\ \frac{16+8i-12i-6i^2}{4-i^2} &= \\ \frac{16-4i+6}{4+1} &= \\ \frac{22-4i}{5} &= \frac{22}{5} - \frac{4}{5}i \end{aligned}$$

2. (3 points) Evaluate the discriminant of the quadratic equation. Use the value of the discriminant to determine whether the quadratic equation has 2 real solutions, 1 repeated real solution, or 2 nonreal complex solutions.

$$16x^2 = 8x - 1$$
$$16x^2 - 8x + 1 = 0 \quad a = 16, b = -8, c = 1$$

$$\begin{aligned} \text{discriminant} &= b^2 - 4ac \\ &= (-8)^2 - 4(16)(1) \\ &= 64 - 64 \\ &= 0 \rightarrow \text{there is } \underline{\text{1}} \text{ repeated real solution} \end{aligned}$$

3. (4 points) Solve the rational equation.

$$\frac{4}{x+3} + \frac{x}{x-5} = 1$$

Domain: $x \neq -3, 5$

LCD: $(x+3)(x-5)$

$$(x+3)(x-5)\left(\frac{4}{x+3}\right) + (x+3)(x-5)\left(\frac{x}{x-5}\right) = 1(x+3)(x-5)$$

$$4(x-5) + (x+3)(x) = x^2 - 2x - 15$$

$$4x - 20 + x^2 + 3x = x^2 - 2x - 15$$

$$9x = 5$$

$$x = \frac{5}{9}$$