

# Outline of Topology

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## Metric Spaces

Real Line  
Least Upper Bound Principle  
Archimedes Principle  
Bolzano-Weierstrass Theorem  
Decimal Representation  
Countability  
Uncountability  
Power set  
Rational numbers  
Algebraic numbers  
Cantor diagonal argument  
Open set  
Closed set  
Closure of a set  
Convergence  
Continuity  
Connectedness  
Interval  
Sharkovsky theorem  
Markov graphs  
Counting periodic points  
Chain connectedness theorem  
Connected open subset of  $\mathbb{R}^n$  is arcwise connected  
Cantor set  
Map of Cantor set onto interval  
Map of Cantor set onto  $[0,1]^n$   
Map of  $[0,1]$  onto  $[0,1]^n$   
Sequential compactness  
Uniform continuity  
Nested intersection of compact connected sets  
Dyadic solenoid  
Homeomorphism  
Embedding  
Equivalent metrics  
Product metric  
Quotient space  
Contraction Mapping Theorem  
Baire Category Theorem

## General Topological spaces

Topology  
Base for a topology  
Hausdorff  
Normal  
Urysohn Lemma  
The M-test  
Uniform convergence of functions  
Uniform convergence of continuous functions is continuous  
Tietze Extension Theorem  
Urysohn metrization theorem  
Compactness  
Finite Intersection Property  
Compact Hausdorff is normal  
Baire Category for compact Hausdorff  
Sorgenfrey line  
Compact subsets of Sorgenfrey line  
Product space, infinite product space  
Quotient spaces  
Cone of a space  
Cone of the integers  
Mapping cylinder  
Mapping torus