

1. Find the unknown variables  $a, b$  such that the following function becomes continuous.

$$f(x) = \begin{cases} a|x - 2| + 3 & \text{if } x < 1 \\ 5 & \text{if } x = 1 \\ bx^2 - 1 & \text{if } x > 1 \end{cases} \quad (1)$$

Hint: A function  $f$  is continuous if at  $x=1$  if both left and right limit at this point exist and they match the value of  $f(1)$ . Please note that for  $a|x - 2| + 3$  some how you should get rid of the absolute value sign. Pay attention to the interval  $x < 1$  and the sign of  $|x - 2|$  at this interval. We had a similar problem in our last discussion quiz!

2. Find the limit.

$$\lim_{x \rightarrow 0} \frac{1 - \cos(2x)}{5x^2} \quad (2)$$

hint: Please note that  $\cos(2x) = \cos^2(x) - \sin^2(x) = 2\cos^2(x) - 1 = 1 - 2\sin^2(x)$ . You can use one of these equivalences for  $\cos(2x)$  and use the fact  $\lim_{t \rightarrow 0} \frac{\sin(t)}{t} = 1$  in order to evaluate this limit.

3. Find all vertical and horizontal asymptotes of the following function.

$$f(x) = \frac{7x - 1}{x^2 - 6x - 16} \quad (3)$$