

$$(1) \mathcal{L}\{1\} = 1/s; \quad s > 0.$$

$$(2) \mathcal{L}[e^{at}] = \frac{1}{s-a}; \quad s > a.$$

$$(3) \mathcal{L}[t^n] = \frac{n!}{s^{n+1}}; \quad s > 0.$$

$$(4) \mathcal{L}[\sin(bt)] = \frac{b}{s^2 + b^2}; \quad s > 0.$$

$$(5) \mathcal{L}[\cos(bt)] = \frac{s}{s^2 + b^2}; \quad s > 0.$$

$$(6) \mathcal{L}[\cosh(bt)] = \frac{s}{s^2 - b^2}; \quad s > b.$$

$$(7) \mathcal{L}[\sinh(bt)] = \frac{b}{s^2 - b^2}; \quad s > b.$$

$$(8) \mathcal{L}[e^{at}f(t)](s) = \mathcal{L}[f](s-a).$$

$$(9) \mathcal{L}[e^{at}\sin(bt)] = \frac{b}{(s-a)^2 + b^2}; \quad s > a.$$

$$(10) \mathcal{L}[e^{at}\cos(bt)] = \frac{s-a}{(s-a)^2 + b^2}; \quad s > a.$$

$$(11) \mathcal{L}[e^{at}t^n] = \frac{n!}{(s-a)^{n+1}}; \quad s > a.$$

$$(12) \mathcal{L}[u(t-a)] = \frac{e^{-as}}{s}.$$

$$(13) \mathcal{L}[u(t-a)f(t-a)](s) = e^{-as}\mathcal{L}[f(t)](s).$$

$$(14) \mathcal{L}[u(t-a)f(t)](s) = e^{-as}\mathcal{L}[f(t+a)](s).$$

$$(15) \mathcal{L}[f(ct)] = \frac{1}{c}\mathcal{L}[f(\frac{t}{c})].$$

$$(16) \mathcal{L}[f \star g](s) = \mathcal{L}[\int_0^t f(t-\tau)g(\tau)d\tau] = \mathcal{L}[f]\mathcal{L}[g].$$

$$(17) \mathcal{L}[\delta(t-a)] = e^{-as}.$$

$$(18) \mathcal{L}[f^{(n)}] = s^n \mathcal{L}[f] - s^{n-1}f(0) - \dots - sf^{(n-2)}(0) - f^{(n-1)}(0).$$

$$(19) \mathcal{L}[y''] = s^2 \mathcal{L}[y] - sy(0) - y'(0). \quad \mathcal{L}[y'] = s\mathcal{L}[y] - y(0).$$

$$(20) \mathcal{L}[(-t)^n f(t)] = \frac{d^n}{ds^n}(\mathcal{L}[f]).$$

$$(21) \mathcal{L}[t \sin(bt)] = \frac{2bs}{(s^2 + b^2)^2}; \quad s > 0.$$

$$(22) \mathcal{L}[t \cos(bt)] = \frac{s^2 - b^2}{(s^2 + b^2)^2}; \quad s > 0.$$

$$(23) \text{ If } f \text{ is periodic of period } T, \text{ then } \mathcal{L}[f](s) = \frac{1}{1 - e^{-sT}} \int_0^T e^{-st} f(t) dt.$$