

## Formulas of possible use

|                     |                                   |                                       |                                                      |
|---------------------|-----------------------------------|---------------------------------------|------------------------------------------------------|
| $\sin 2x$           | $= 2 \sin x \cos x$               | $\mathcal{L}\{t^n\}$                  | $= \frac{n!}{s^{n+1}}$                               |
| $\cos 2x$           | $= \cos^2 x - \sin^2 x$           | $\mathcal{L}\{e^{at}\}$               | $= \frac{1}{s-a}$                                    |
| $\sin^2 x$          | $= \frac{1 - \cos 2x}{2}$         | $\mathcal{L}\{\sin bt\}$              | $= \frac{b}{s^2 + b^2}$                              |
| $\cos^2 x$          | $= \frac{1 + \cos 2x}{2}$         | $\mathcal{L}\{\cos bt\}$              | $= \frac{s}{s^2 + b^2}$                              |
| $\sin(x+y)$         | $= \sin x \cos y + \cos x \sin y$ | $\mathcal{L}\{e^{at}f(t)\}$           | $= F(s-a), \text{ where } F(s) = \mathcal{L}\{f\}.$  |
| $\cos(x+y)$         | $= \cos x \cos y - \sin x \sin y$ | $\mathcal{L}\{tf(t)\}$                | $= -\frac{d}{ds}\mathcal{L}\{f\}$                    |
| $\int \tan u \, du$ | $= -\ln  \cos u $                 | $\mathcal{L}\{f'(t)\}$                | $= s\mathcal{L}\{f\} - f(0)$                         |
| $\int \cot u \, du$ | $= \ln  \sin u $                  | $\mathcal{L}\{u(t-a)f(t)\}$           | $= e^{-as}\mathcal{L}\{f(t+a)\}$                     |
| $\int \sec u \, du$ | $= \ln  \sec u + \tan u $         | $\mathcal{L}\{f, \text{ period } T\}$ | $= \frac{\mathcal{L}\{f_T\}}{1 - e^{-sT}}$           |
| $\int \csc u \, du$ | $= \ln  \csc u - \cot u ,$        | $\mathcal{L}\{\delta(t-a)\}$          | $= e^{-as}$                                          |
|                     |                                   | $\mathcal{L}\{f * g\}$                | $= \mathcal{L}\{f\} \mathcal{L}\{g\}, \text{ where}$ |
|                     |                                   | $f * g$                               | $= \int_0^t f(t-v)g(v) \, dv$                        |

## Variation of parameters

$ay'' + by' + cy = f(t)$  has solution  $y(t) = C(t)y_1(t) + D(t)y_2(t)$  where

$$C = \int \frac{-fy_2}{a(y_1y_2' - y_2y_1')} dt$$

$$D = \int \frac{fy_1}{a(y_1y_2' - y_2y_1')} dt$$