

Speaker: Peter Cholak

Title: Encodable by thin sets

Abstract: Let c be a coloring of n -tuples of ω by finitely many colors. For l less than the number of colors, a set T is *l-thin* iff c uses at most l colors to color all the n -tuples from T . The statement such a thin set exists is called $RT^{n}_{<\infty, l}$.

We say a set S is $RT^{n}_{<\infty, l}$ -*encodable* iff there is a coloring c as above such that every l -thin set computes S . Wang showed that when l is "large" only the computable sets are $RT^{n}_{<\infty, l}$ -encodable. Dorais, Dzhafarov, Hirst, Miletic, and Shafer showed that the hyperarithmetic sets are $RT^{n}_{<\infty, l}$ -encodable for "small" l . Cholak and Patey showed that the arithmetic sets are $RT^{n}_{<\infty, l}$ -encodable for "medium" l . Of course, what is missing here is the exact definition of small, medium, and large. In the talk we will provide "tight" definitions, at least, for a "few" n . This is joint work with Ludovic Patey.