

### Exam 1.

The solutions are due Wednesday February 7th before class. Either bring them to class, or send them by e-mail to my address (preferably in pdf).

1. Provide an example of formulas  $A, B$  in sentential logic such that  $A \vdash B$  holds and at the same time  $B \vdash A$  does not hold. Justify your answer.
2. Provide a formal proof of  $A \rightarrow B \vdash \neg B \rightarrow \neg A$  in the natural deduction calculus for sentential logic.
3. Consider the sentence  $\forall x \exists y \forall z (\neg x R z) \rightarrow x R y$  in the language with one special binary symbol  $R$ . Produce a structure in which this sentence holds.
4. Consider the language  $L$  with one special binary functional symbol for multiplication. (No addition or ordering or constants.) Lookk at the following three  $L$ -structures: rationals with multiplication, reals with multiplication, and the complex numbers with multiplication. For each one, find an  $L$ -sentence which is satisfied in it but not in the others.