Abstract: Remmel showed that a computable linear order $L$ is computably categorical if and only if the order type of $L$ has only a finite number of successivities. As part of the proof, Remmel assumes that $L$ has infinitely many successivities and constructs another computable linear order $R$, which is not computably isomorphic to $L$, and a $\Delta^0_2$-isomorphism $f$ such that $f : L \rightarrow R$ is an isomorphism. Hence showing that $L$ is not computably categorical. In this talk I will discuss the conditions under which we can use permitting arguments to construct $f$ below certain types of $\Delta^0_2$ degrees.